

A Novel Adaptive Dragonfly Algorithm for Global Optimization Problems

Naveen Sihag¹ Ph.D. Scholar)

Department of Computer Engineering, Rajasthan Technical University Kota, Rajasthan 324002, India¹

Corresponding Author: Naveen Sihag

ABSTRACT: A novel bio-inspired optimization algorithm based on the swarming behavior of Dragonflies in nature named as Dragonfly Algorithm (DA) in contrast to meta-heuristics; main feature is randomization having a relevant role in both exploration and exploitation in optimization problem. A novel randomization technique termed adaptive technique is integrated with DA and exercised on unconstrained test benchmark function and localization of partial discharge in transformer like geometry. DA algorithm has quality feature that it uses static and dynamic swarming process covers vast area in exploration phase and step position changes over each iteration towards targeted destination or towards optimal solution. Integration of new randomization adaptive technique provides potential that ADA algorithm to attain global optimal solution and faster convergence with less parameter dependency. Adaptive DA (ADA) solutions are evaluated and results shows its competitively better performance over standard DA optimization algorithms.

KEYWORDS: Meta-heuristic; Dragonfly Algorithm; Adaptive technique; Global optimal; Acoustic; Sensor.

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I. Introduction

A novel nature –inspired, Dragonfly algorithm [1] based on the swarming behavior. A dragonfly in nature consists of two type swarming behavior Static swarm and dynamic swarm. In static swarm Dragonflies makes small groups and fly in search of food similar exploration phase and dynamic swarm at the time of attack on food and for migration to other place shows exploitation phase in optimization problem.

In the meta-heuristic algorithms, randomization play a very important role in both exploration and exploitation where more strengthen randomization techniques are Markov chains, Levy flights and Gaussian or normal distribution and new technique is adaptive technique. So meta-heuristic algorithms on integrated with adaptive technique results in less computational time to reach optimum solution, local minima avoidance and faster convergence.

In past, many optimization algorithms based on gradient search for solving linear and non-linear equation but in gradient search method value of objective function and constraint unstable and multiple peaks if problem having more than one local optimum.

Population based DA is a meta-heuristic optimization algorithm has an ability to avoid local optima and get global optimal solution that make it appropriate for practical applications without structural modifications in algorithm for solving different constrained or unconstrained optimization problems. DA integrated with adaptive technique reduces the computational times for highly complex problems.

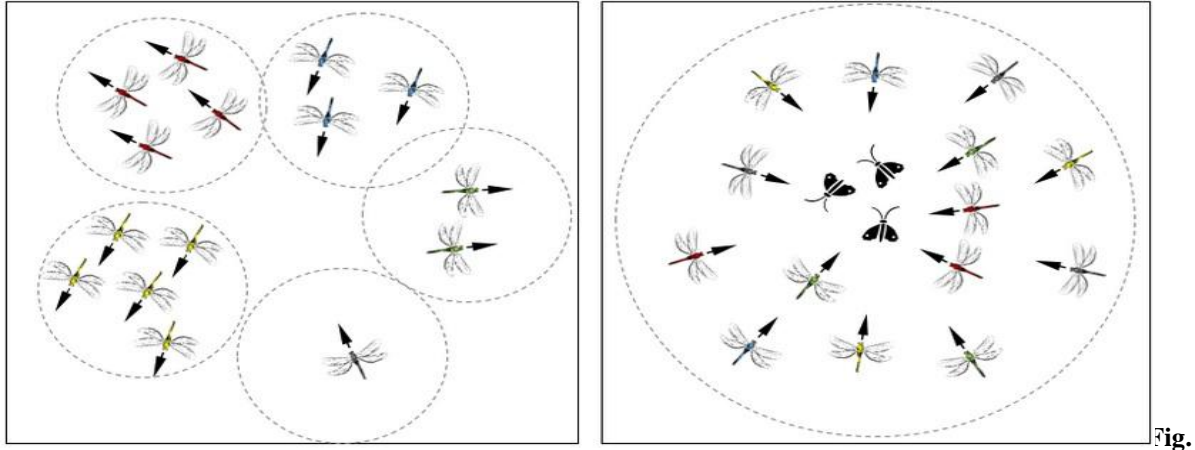
Paper under literature review are: Adaptive Cuckoo Search Algorithm (ACSA) [2] [3], QGA [4], Acoustic Partial discharge (PD)[5] [6], HGAPSO [7], PSACO [8], HSABA [9], PBILKH [10], KH-QPSO [11], IFA-HS [12], HS/FA [13], CKH [14], HS/BA [15], HPSACO [16], CSKH [17], HS-CSS [18], PSOHS [19], DEKH [20], HS/CS [21], HSBBO [22], CSS-PSO [23] etc.

Recently trend of optimization is to improve performance of meta-heuristic algorithms [24] by integrating with chaos theory, Levy flights strategy, Adaptive randomization technique, Evolutionary boundary handling scheme, and genetic operators like as crossover and mutation. Popular genetic operators used in KH [25] that can accelerate its global convergence speed. Evolutionary constraint handling scheme is used in Interior Search Algorithm (ISA) [26] that avoid upper and lower limits of variables.

The remainder of this paper is organized as follows: The next Section describes the Dragonfly algorithm and its algebraic equations are given in Section 2. Section 3 includes description of Adaptive technique. Section 4 consists of simulation results of unconstrained benchmark test function, convergence curve and tables of results compared with source algorithm. In Section 5 PD localization by acoustic emission in section 6 conclusion is drawn. Finally, acknowledgment gives regards detail and at the end, references are written.

II. Dragonfly Algorithm

Dragonfly Algorithm proposed by Seyedali Mirjalili, inspired from natural swarming behavior of Dragonflies which makes small group and fly different direction covers vast area in search of food technically term in optimization is exploration phase and makes large group to shift other place termed similar exploitation phase, called static and dynamic swarm.



1: Dynamic versus Static dragonfly swarms

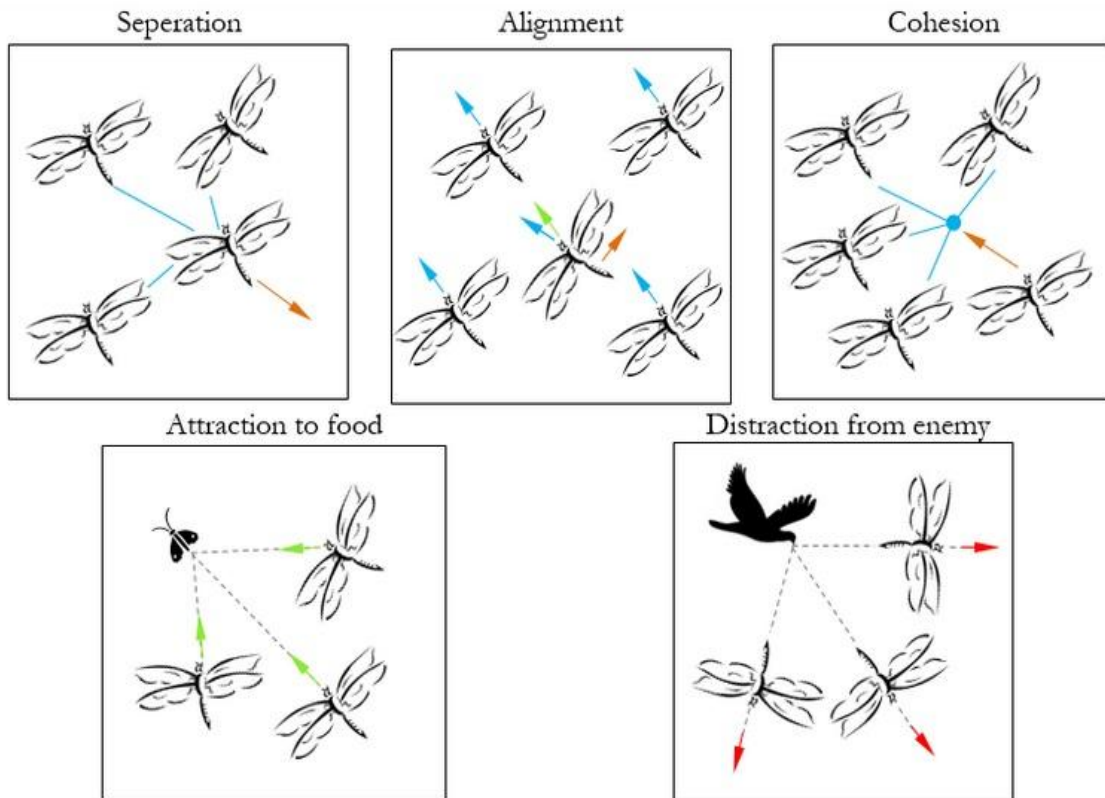


Fig. 2: Dragonfly Algorithm principle

Each portion of Dragonfly Algorithm is formulated by algebraic equations are:

1. For Separation part formulating equation:

$$S_i = - \sum_{j=1}^N X - X_j \quad (1)$$

2. For Alignment part formulating equation:

$$A_i = \frac{\sum_{j=1}^N X_j}{N} \quad (2)$$

3. For cohesion part formulating equation:

$$C_i = \frac{\sum_{j=1}^N X_j}{N} - X \quad (3)$$

4. For Attraction towards a food source part formulating equation:

$$F_i = X^+ - X \quad (4)$$

5. For Attraction towards a food source part formulating equation:

$$E_i = X^- + X \quad (5)$$

6. Step vector is formulating equation:

$$\Delta X_{t+1} = (sS_i + aA_i + cC_i + fF_i + eE_i) + w\Delta X_t \quad (6)$$

7. Position vector is calculated using equation

$$X_{t+1} = X_t + \Delta X_{t+1} \quad (7)$$

8. Position of dragonfly updated using equation

$$X_{t+1} = X_t + \text{Levy}(x) * X_t \quad (8)$$

Where

Where X =Location of the current individuals, N = Neighboring individuals, X^+ =positions of food source, X^- =positions of enemy, s =separation weight, a =alignment weight, c =cohesion weight, f =food weight, e =enemy weight, w =inertia weight, t =iteration counter and d =dimension of position vectors that levy flight step calculated.

III. Adaptive Dragonfly Algorithm

In the meta-heuristic algorithms, randomization play a very important role in both exploration and exploitation where more randomization techniques are Markov chains, Levy flights and Gaussian or normal distribution and new technique is adaptive technique. Adaptive technique used by Pauline Ong in Cuckoo Search Algorithm (CSA) [2] and shows improvement in results of CSA algorithms. The Adaptive technique [3] includes best features like it consists of less parameter dependency, not required to define initial parameter and step size or position towards optimum solution is adaptively changes according to its functional fitness value over the course of iteration. So meta-heuristic algorithms on integrated with adaptive technique results in less computational time to reach optimum solution, local minima avoidance and faster convergence.

$$X_i^{t+1} = X_i^t + \text{randn} * \left(\frac{1}{t}\right)^{\left| \frac{(bestf(t) - fi(t))}{(bestf(t) - worstf(t))} \right|} \quad (9)$$

Where

X_i^{t+1} new solution of i -th dimension in t -th iteration $f(t)$ is the fitness value

IV. Simulation Results For Unconstraint Test Benchmark Function

Table 1: Benchmark Test functions

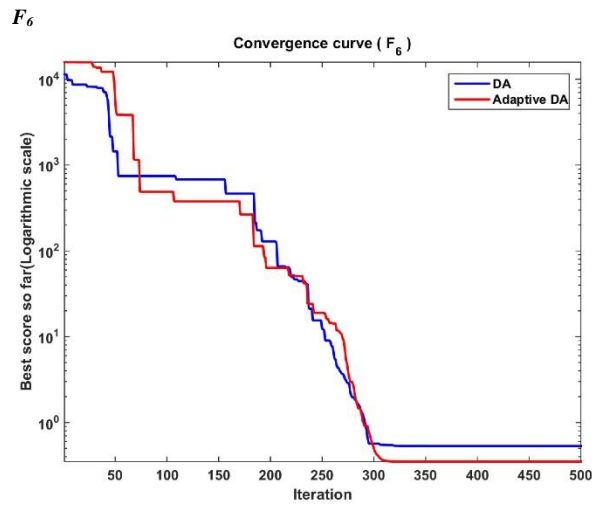
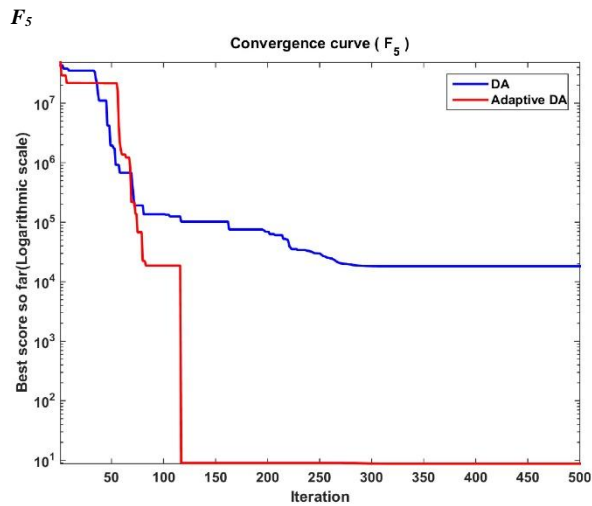
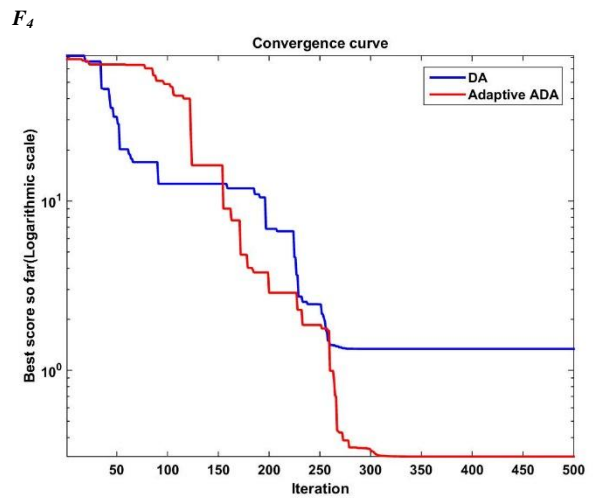
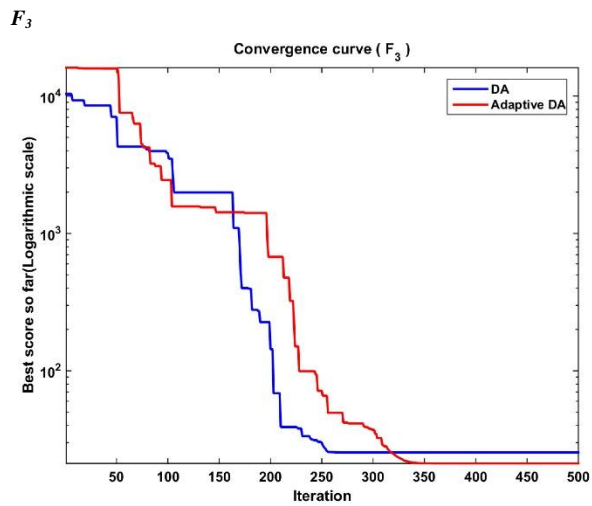
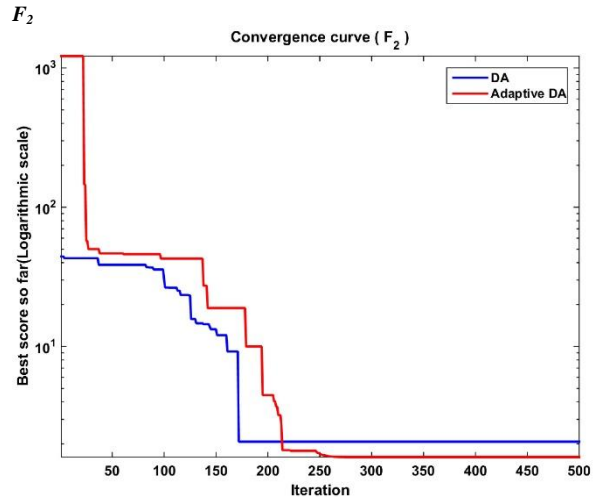
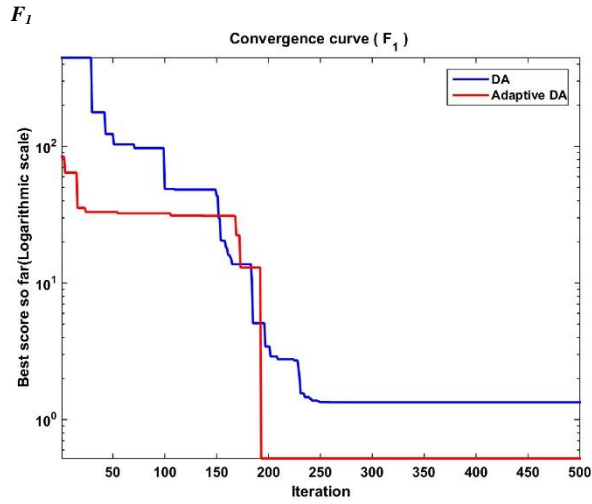
No.	Name	Function	Dim	Range	Fmin
F1	Sphere	$f(x) = \sum_{i=1}^n x_i^2 * R(x)$	10	[-100, 100]	0
F2	Schwefel 2.22	$f(x) = \sum_{i=1}^n x_i + \prod_{i=1}^n x_i * R(x)$	10	[-10, 10]	0
F3	Schwefel 1.2	$f(x) = \sum_{i=1}^n \left(\sum_{j=1}^i x_j \right)^2 * R(x)$	10	[-100, 100]	0
F4	Schwefel 2.21	$f(x) = \max_i \{ x_i , 1 \leq i \leq n\}$	10	[-100, 100]	0

F5	Rosenbrock's Function	$f(x) = \sum_{i=1}^{n-1} \left[100(x_{i+1} - x_i^2)^2 + (x_i - 1)^2 \right]$	10	[-30, 30]	0
F6	Step Function	$f(x) = \sum_{i=1}^n ([x_i + 0.5])^2 * R(x)$	10	[-100, 100]	0
F7	Quartic Function	$f(x) = \sum_{i=1}^n i x_i^4 + \text{random}[0,1] * R(x)$	10	[-1.28, 1.28]	0
F8	Schwefel 2.26	$F(x) = \sum_{i=1}^n -x_i \sin(\sqrt{ x_i }) * R(x)$	10	[-500, 500]	(-418.9829*5)
F9	Rastrigin	$F(x) = \sum_{i=1}^n [x_i^2 - 10 \cos(2\pi x_i) + 10] * F$	10	[-5.12, 5.12]	0
F10	Ackley's Function	$F(x) = -20 \exp\left(-0.2 \sqrt{\frac{1}{n} \sum_{i=1}^n x_i^2}\right) - \exp\left(\frac{1}{n} \sum_{i=1}^n \cos(2\pi x_i)\right) + 20 + e * R(x)$	10	[-32, 32]	0
F11	Griewank Function	$F(x) = \frac{1}{4000} \sum_{i=1}^n x_i^2 - \prod_{i=1}^n \cos\left(\frac{x_i}{\sqrt{i}}\right) + 1 * R(x)$	10	[-600, 600]	0
F12	Penalty 1	$F(x) = \frac{\pi}{n} \left\{ \begin{aligned} &10 \sin(\pi y_1) + \sum_{i=1}^{n-1} (y_i - 1)^2 \\ &[1 + 10 \sin^2(\pi y_{i+1})] + (y_n - \end{aligned} \right.$ $y_i = 1 + \frac{x_i + 1}{4},$ $u(x_i, a, k, m) = \begin{cases} k(x_i - a)^m & -a < . \\ 0 & \\ k(-x_i - a)^m & ; \end{cases}$	10	[-50, 50]	0
F13	Penalty 2	$F(x) = 0.1 \left\{ \begin{aligned} &\sin^2(3\pi x_1) + \sum_{i=1}^n (x_i - 1)^2 \\ &[1 + \sin^2(3\pi x_i + 1)] \\ &+ (x_n - 1)^2 [1 + \sin^2(2\pi x_n \end{aligned} \right.$ $+ \sum_{i=1}^n u(x_i, 5, 100, 4) * R(x)$	10	[-50, 50]	0

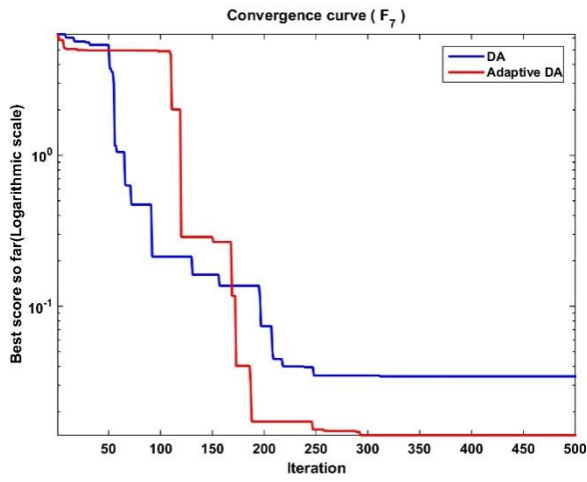
F14	De (Shekel's Foxholes)	Joung	$F(x) = \left(\frac{1}{500} + \sum_{j=1}^{25} \frac{1}{j + \sum_{i=1}^2 (x_i - a_{ij})^6} \right)^{-1}$	2	[-65.536, 65.536]	1
F15	Kowalik's Function		$f(x) = \sum_{i=1}^{11} a_i - \left[\frac{x_i (b_i^2 + b_i x_2)}{b_i^2 + b_i x_3 + x_4} \right]^2$	4	[-5,5]	0.0003 0
F16	Shekel		$f(x) = - \sum_{i=1}^{10} \left[(X - a_i)(X - a_i)^T + c_i \right]^{-1}$	4	[0,10]	-10.536 3
F17	Cube function		$f(x) = 100(x_2 - x_1^3)^2 + (1 - x_1)^2$	30	[-100, 100]	0
F18	Matyas function		$f(x) = 0.26(x_1^2 + x_2^2) - 0.48x_1x_2$	10	[-30, 30]	0
F19	Powell function		$f(x) = \sum_{i=1}^{D-2} \left\{ \begin{array}{l} (x_{i-1} + 10x_i)^2 + 5(x_{i+1} - x_{i+2}) \\ (x_i - 2x_{i+1})^4 + 10(x_{i-1} - x_{i+2}) \end{array} \right.$	4	[-30, 30]	0
F20	Beale Function		$f(x) = \left\{ \begin{array}{l} (1.5 - x_1 + x_1 x_2)^2 + (2.25 - x_1 + \\ + (2.625 - x_1 + x_1 x_2^3)^2 \end{array} \right.$	30	[-100, 100]	0
F21	levy13 function		$f(x) = \left\{ \begin{array}{l} \sin^2(3\pi x_1) + (x_1 - 1)^2 (1 + \sin^2(\\ + (x_2 - 1)^2 (1 + \sin^2(2\pi x_2)) \end{array} \right.$	30	[-10, 10]	0

Table 2: Internal Parameters

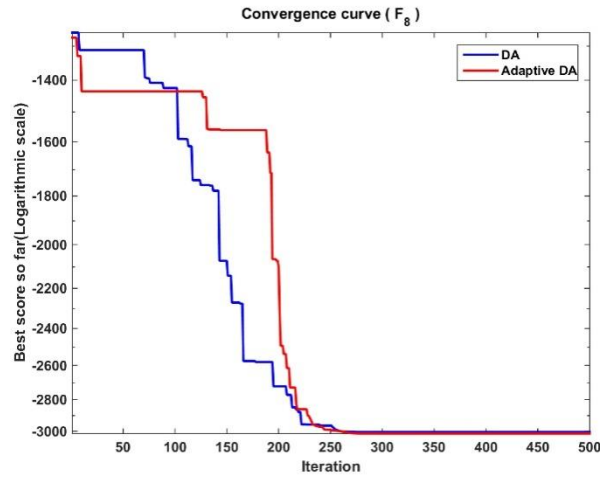
Parameter Name	Search Agents no.	Max. Iteration no.	No. of Evolution
F1-F17, F20-F21	30	500	20-30
F18	10	100	20-30
F19	30	200	20-30
Acoustic Localization	PD 40	200	20
Note:- Scale specified on axis, Not specified means axis are linear scale			



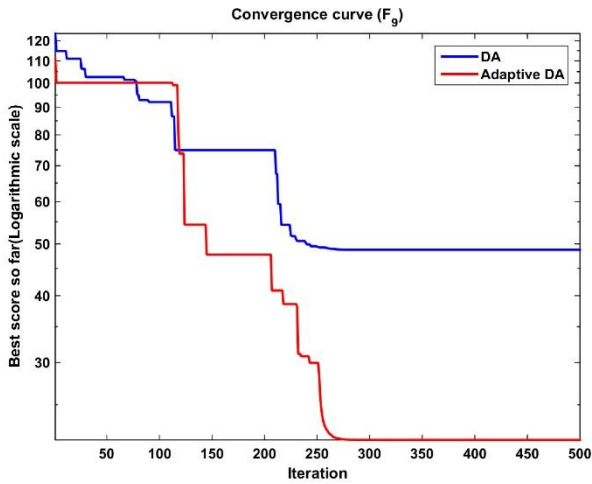
F_7



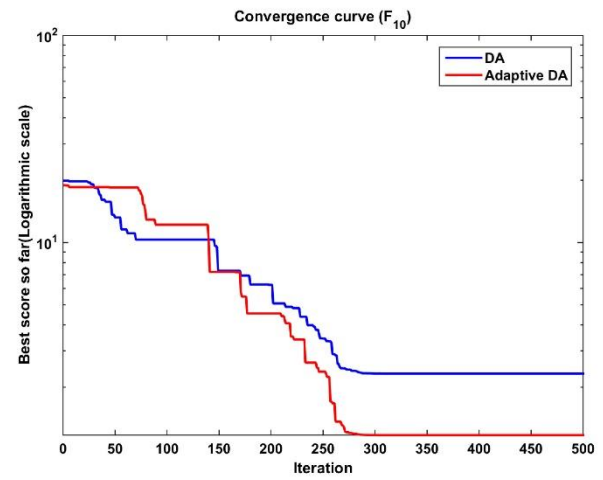
F_8



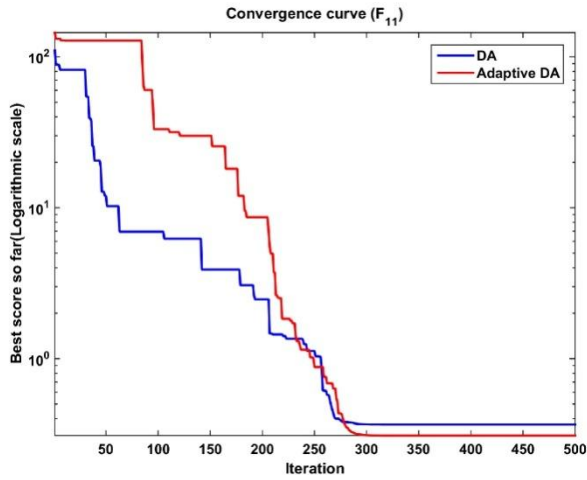
F_9



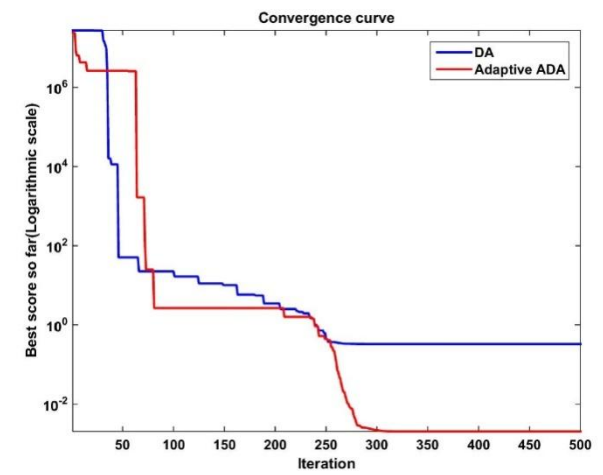
F_{10}



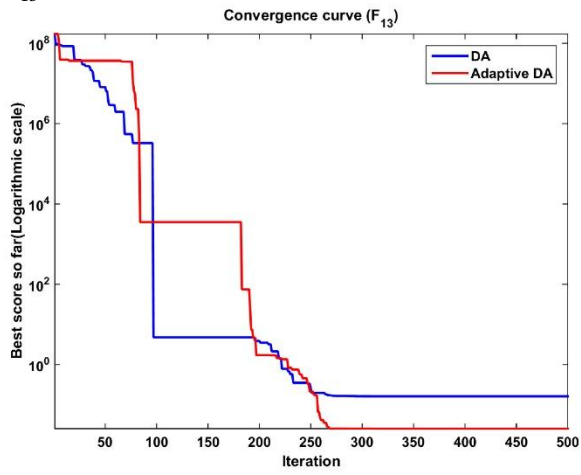
F_{11}



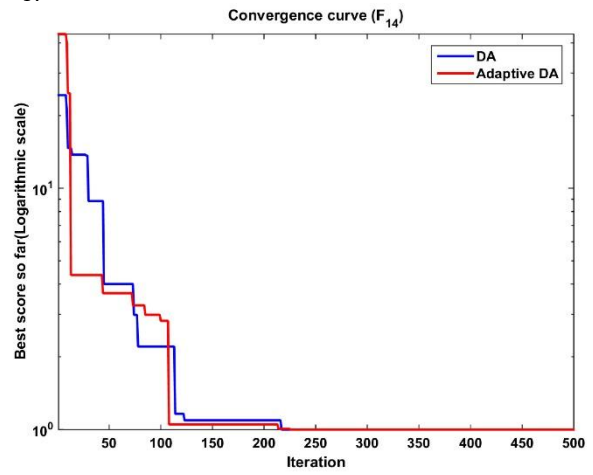
F_{12}



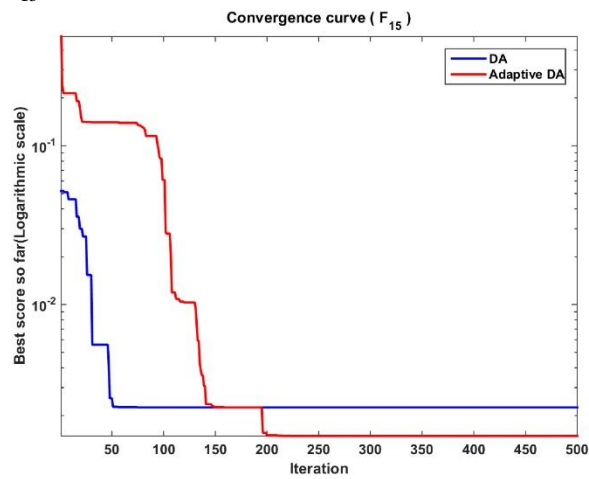
F_{13}



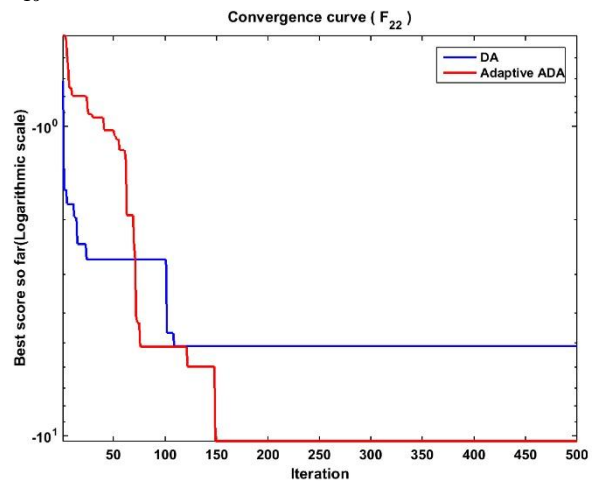
F_{14}



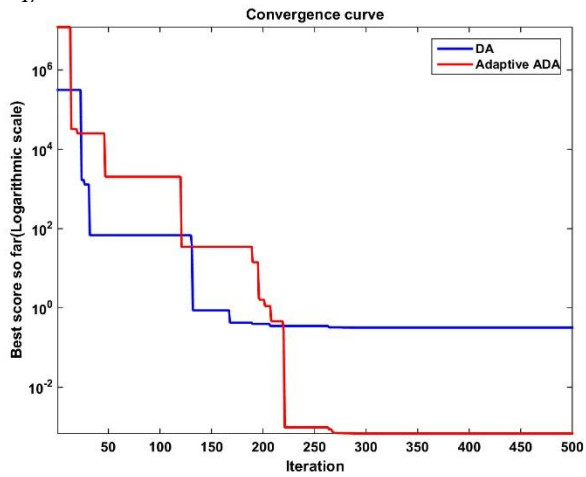
F_{15}



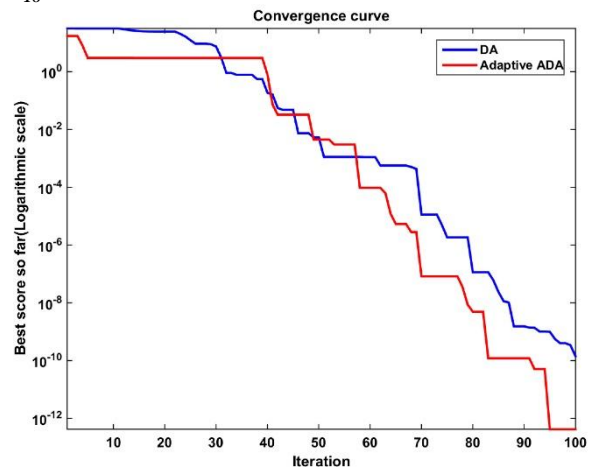
F_{16}



F_{17}



F_{18}



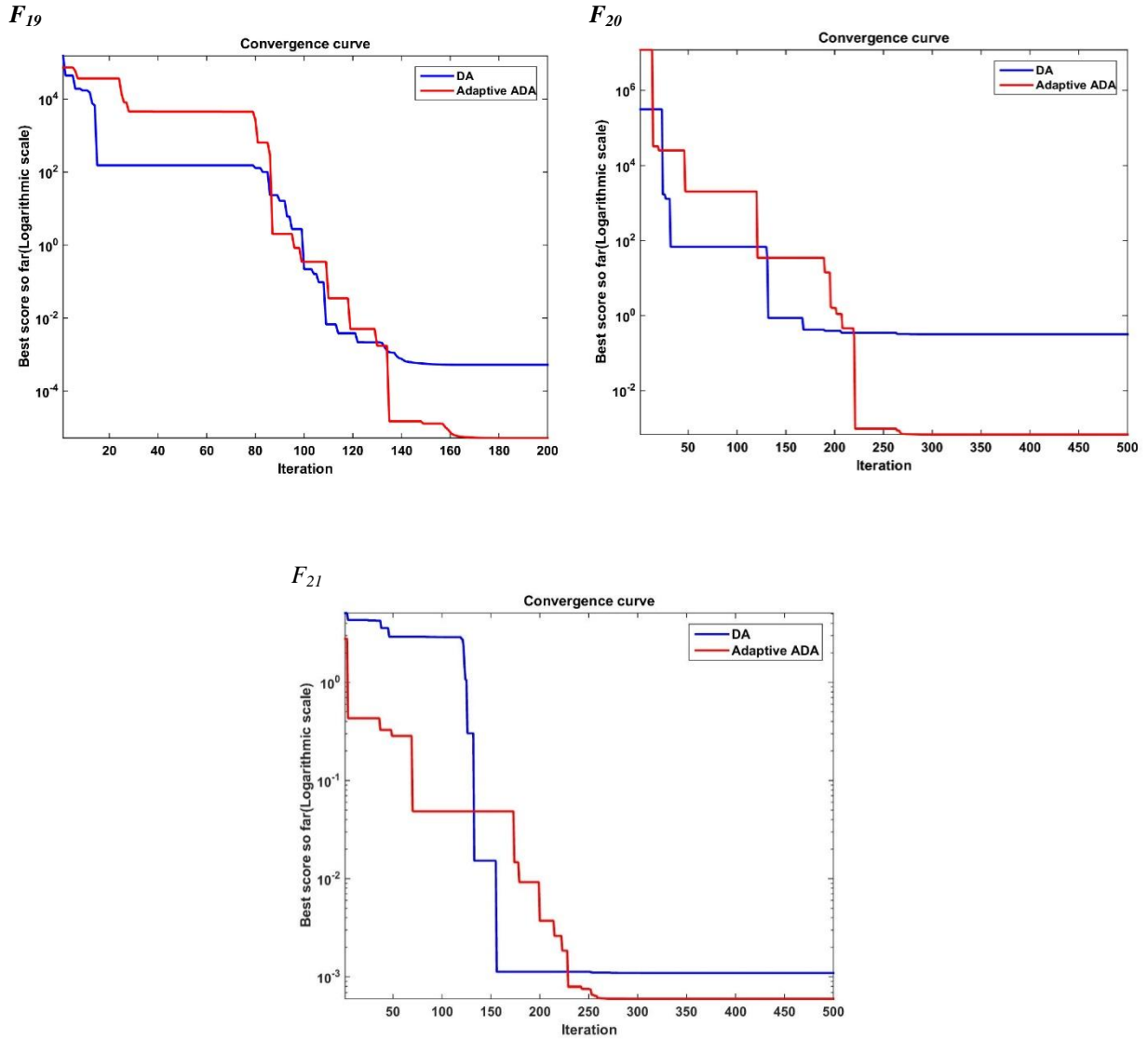


Fig. 3: Convergence Curve of Benchmark Test Function

Table 3: Result for benchmark functions

Fun.	Dragonfly Algorithm (DA)			Adaptive Dragonfly Algorithm (ADA)		
	Ave	Best	S.D.	Ave	Best	S.D.
F1	1.6625	1.3402	0.45582	1.7522	0.51981	1.7429
F2	2.0871	2.0731	0.019856	2.052	1.6064	0.6301
F3	195.5395	25.4491	240.5442	52.0969	21.1825	43.7196
F4	2.2896	1.3361	1.3485	2.8441	0.30896	3.5853
F5	24058.9814	18222.1745	18222.174	9.4869	8.7653	1.0205
F6	2.425	0.53177	2.6774	4.3229	0.35012	5.6183
F7	0.036	0.034331	0.0023597	0.021189	0.014004	0.010162
F8	-2940.1704	-3005.11	91.8386	2526.0036	-3014.8973	691.4002
F9	49.9072	48.7586	1.6244	22.6842	21.4892	1.69
F10	2.574	2.3276	0.34844	2.1084	1.1751	1.3199
F11	0.48509	0.36625	0.16807	0.45095	0.30942	0.20017
F12	1.2058	0.32764	1.2419	1.3524	0.002022	1.9098

F13	0.57324	0.16349	0.57948	3.7987	0.025623	5.3359
F14	0.998	0.998	1.5701E-16	0.998	0.998	1.0943E-11
F15	0.0052928	0.0022519	0.0043004	0.0014887	0.0014887	1.1208E-07
F16	-3.7751	-5.1285	1.914	-7.856	-10.5364	3.7906
F17	1.5413	0.094384	2.0463	0.356	0.054492	0.42639
F18	1.679E-10	1.4179E-10	3.6931E-11	1.1675E-10	4.2141E-13	1.6452E-10
F19	0.0014206	0.0010947	0.00046089	0.0010075	0.00060453	0.00056983
F20	0.55184	0.31861	0.32983	0.021091	0.00067904	0.028867
F21	0.0011043	0.00052501	0.00081919	4.0946	5.1662E-06	5.7906

V. Acoustic Pd Localization Sensor Position

Dielectric breakdown in transformers is most frequently initiated by partial discharges. The consequences of these types of occurrences can be hazardous if not detected in a timely fashion. Regular PD analysis gives an accurate indication of the status of the deterioration process. So it is possible to foretell developing fault condition by online monitoring and precautionary tests. It is very much essential to have information of PD level and location to plan maintenance of electrical equipment. A famous method of understanding the health of the transformer is by studying the partial discharge signals. Monitoring of transformer can be either online or offline. The primary established techniques for electrical PD detection by measuring current or Radio Frequency (RF) pulses. Suppression of interference is one of the main challenges in detecting PDs, either while the transformer is off-line or on-line in a noisy environment. The off-line PD detection methods only provide snapshots in time of part of the transformer's condition. On the other hand, no standards have yet been developed for on-line electrical monitoring of PDs.

It is well known that the occurrence of discharge results in discharge current or voltage pulse, electromagnetic impulse radiation, ultrasonic impulse radiation and visible or ultraviolet light emission. Accordingly, there are several detection methods that have been developed to measure those phenomena respectively. Acoustic detection is one of them which is very famous nowadays.

PD generates acoustic waves in range of 20 kHz to 1 MHz. External system and internal system are two categories of acoustic detection techniques based on sensor location in transformer. External system is widely accepted as sensors are mounted outside of the transformer. An obvious advantage of the acoustic method is that it can locate the site of a PD by algorithms. Electromagnetic interference may cause corruption of signals captured by piezoelectric sensors.

A main objective is to determine the position of the PD source based on signals captured by sensor array inside the transformer tank as shown in Fig. 3. Each sensor will capture acoustic signals at different time as shown in Fig. 4. Time Difference of Arrival (TDOA) algorithm has been implemented to find location of partial discharge source.

PDE equation in homogeneous medium for propagation of acoustic wave:

$$\frac{\partial^2 P}{\partial t^2} = v^2 \nabla^2 P = v^2 \left(\frac{\partial^2 P}{\partial x^2} + \frac{\partial^2 P}{\partial y^2} + \frac{\partial^2 P}{\partial z^2} \right) \quad (10)$$

Where: $P(x, y, z, t)$ pressure wave field; function of space and time; x, y, z Cartesian co-ordinates (mm) and v acoustic wave velocity (m/s).

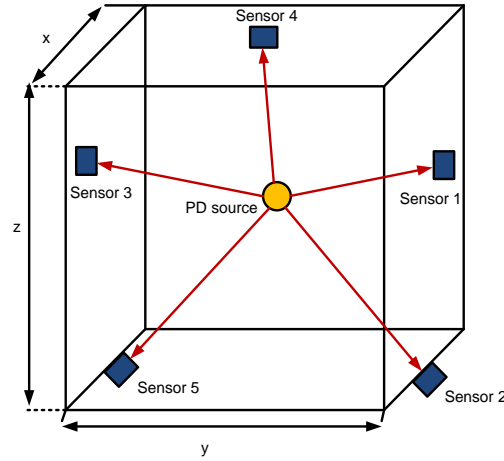


Fig. 4: Visualization of PD source and sensor arrangement

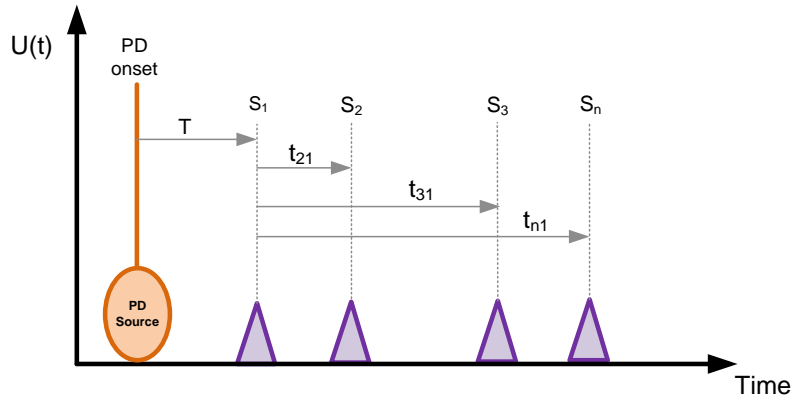


Fig. 5: Schematic of acoustic time differences in reference to electrical PD signal

Table 4: Transformer dimension and Co-ordination position of sensor

Element	X-axis (mm)	Y-axis (mm)	Z-axis (mm)
Transformer Dimension	5000	3000	4000
Actual PD source	4500	2600	3700
Sensor (S ₁)	2500	0	2000
Sensor (S ₂)	2500	1500	4000
Sensor (S ₃)	5000	1500	2000
Sensor (S ₄)	2500	3000	2000
Sensor (S ₅)	0	1500	2000

$t_1 = 2600$ micro-seconds (Reference)

$\tau_{i1} (\mu s) = [1600, 1500, 1900, 3524.69] - t_1$, $i = 2, 3, 4, 5$, And sensor 1 is assumed as reference paper [6].

Problem Formulation:

$$\tau_{21} = -1000 \times 10^{-03}, \tau_{31} = -1100 \times 10^{-03}, \quad (11)$$

$$\tau_{41} = -700 \times 10^{-03}, \tau_{51} = -924.69 \times 10^{-03},$$

$$P = \left[(x - x_1)^2 + (y - y_1)^2 + (z - z_1)^2 \right]^{0.5} \quad (12)$$

$$a = \left[(x - x_2)^2 + (y - y_2)^2 + (z - z_2)^2 \right]^{0.5} - P - v_e \tau_{21}; \quad (13)$$

$$b = \left[(x - x_3)^2 + (y - y_3)^2 + (z - z_3)^2 \right]^{0.5} - P - v_e \tau_{31}; \quad (14)$$

$$c = \left[(x - x_4)^2 + (y - y_4)^2 + (z - z_4)^2 \right]^{0.5} - P - v_e \tau_{41}; \quad (15)$$

$$d = \left[(x - x_5)^2 + (y - y_5)^2 + (z - z_5)^2 \right]^{0.5} - P - v_e \tau_{51}; \quad (16)$$

$$\text{Min } \{D_f(x, y, z, v_e)\} = a^2 + b^2 + c^2 + d^2; \quad (17)$$

Subjected to

$$\left. \begin{aligned} 0 &\leq x \leq x_{\max} \\ 0 &\leq y \leq y_{\max} \\ 0 &\leq z \leq z_{\max} \\ 1200 &\leq v_e \leq 1500, \quad (m/s) \end{aligned} \right\} \quad (18)$$

Where:

$x_{\max}, y_{\max}, z_{\max}$ and v_e are transformer tank dimension and equality sound velocity.

Calculated PD source is $P_c(x_c, y_c, z_c)$ comprehensive distance error of it with actual PD source $P(x, y, z)$ is

$$\Delta R = \left[(x - x_c)^2 + (y - y_c)^2 + (z - z_c)^2 \right]^{0.5} \quad (19)$$

Error of each co-ordinate is formulated:

$$\epsilon_r = \left| \frac{L_{act} - L_{cal}}{L_{act}} \right| \times 100\% \quad (20)$$

Maximum deviation D_{\max}

$$D_{\max} = \max \left\{ \begin{aligned} &|x_{act} - x_{cal}| \\ &|y_{act} - y_{cal}| \\ &|z_{act} - z_{cal}| \end{aligned} \right\} \quad (21)$$

Where; $L_{act}, x_{act}, y_{act}, z_{act}$ and $L_{cal}, x_{cal}, y_{cal}, z_{cal}$ actual and calculated co-ordinates respectively.

Table 5: Comparison of the results of PD localization

Coordinate (mm)	Actual PD source	DA	ADA	GA
X	4500	4381.7461	4382.1807	4223.76
Y	2600	2469.6028	2469.8002	2391.71
Z	3700	3647.4902	3647.9569	3503.04

Table 6: Error analysis

Error	DA	ADA	GA
Error of x%	2.627	2.618	6.14
Error of y%	5.015	5.007	8.01
Error of z%	1.419	1.406	5.32
D_{\max} /mm	130.3972	130.1998	276.24
Comprehensive Error(ΔR /mm)	183.6972	183.1443	398.10

VI. Conclusion

Dragonfly Algorithm have an ability to find out optimum solution with constrained handling which includes both equality and inequality constraints. While obtaining optimum solution constraint limits should not be violated. Randomization plays an important role in both exploration and exploitation. Adaptive technique causes faster convergence, randomness, and stochastic behavior for improving solutions. Adaptive technique also used for random walk in search space when no neighboring solution exists to converse towards optimal solution. Acoustic PD source localization method based on Adaptive Dragonfly Algorithm is feasible. PD localization by ADA gives better result than DA and also accurate in compare to GA. The ADA result of various unconstrained problems proves that it is also an effective method in solving challenging problems with unknown search space.

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